



An earth system's approach to the sensitivity of the water cycle

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26. October 2016

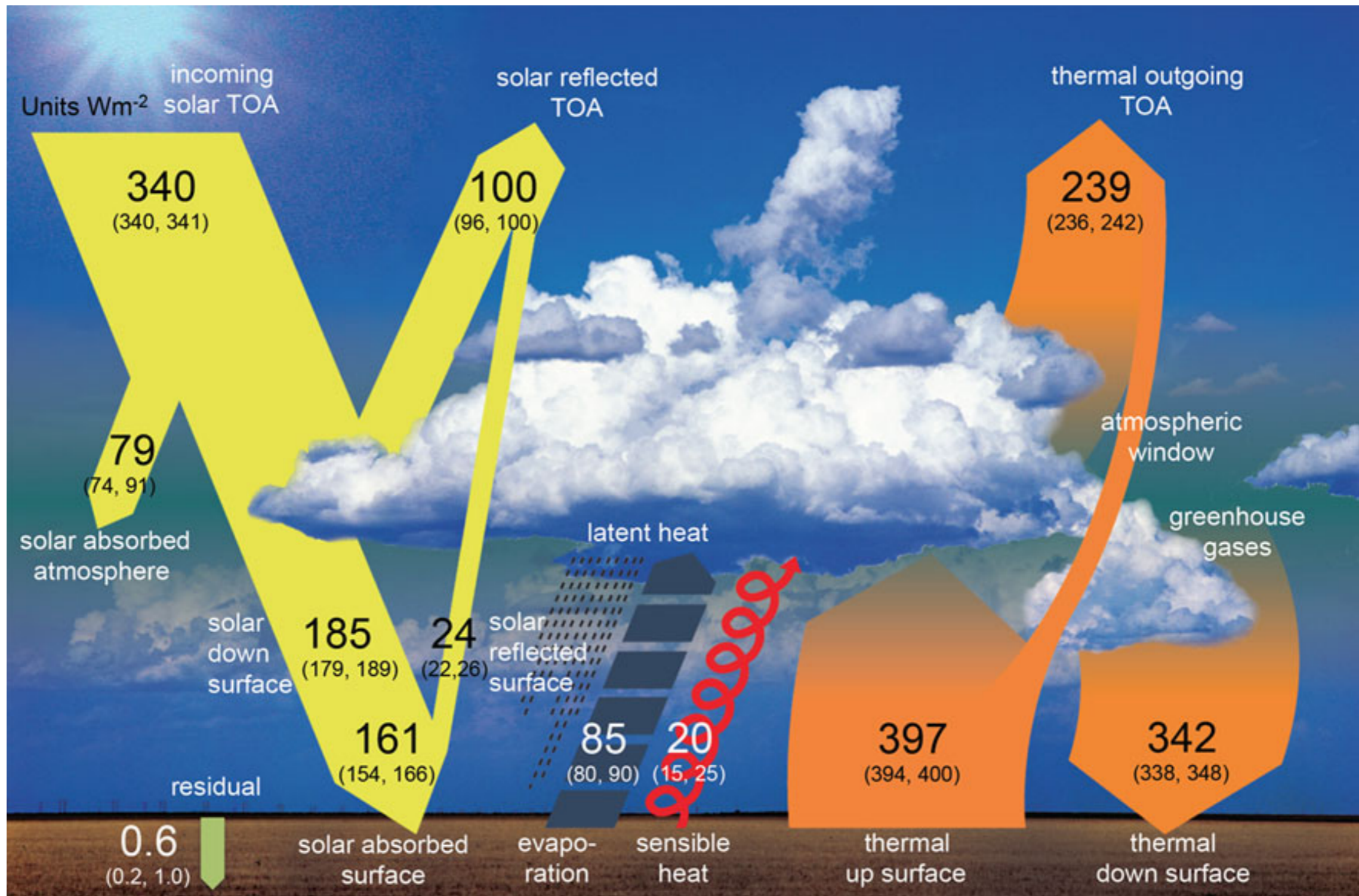
EGU-Leonardo conference on the hydrological cycle, Ourense

catchments as organised systems



Deutsche
Forschungsgemeinschaft

Water cycle ~ radiation and convection



Wild et al 2013, Clim. Dyn

Renner and Kleidon EGU-Leonardo 2016

Systems' perspective on earth

natural system
processes
interacting at
multiple time scales

**Global climate
model**
dynamic state
equations
sub-grid
parameterisations

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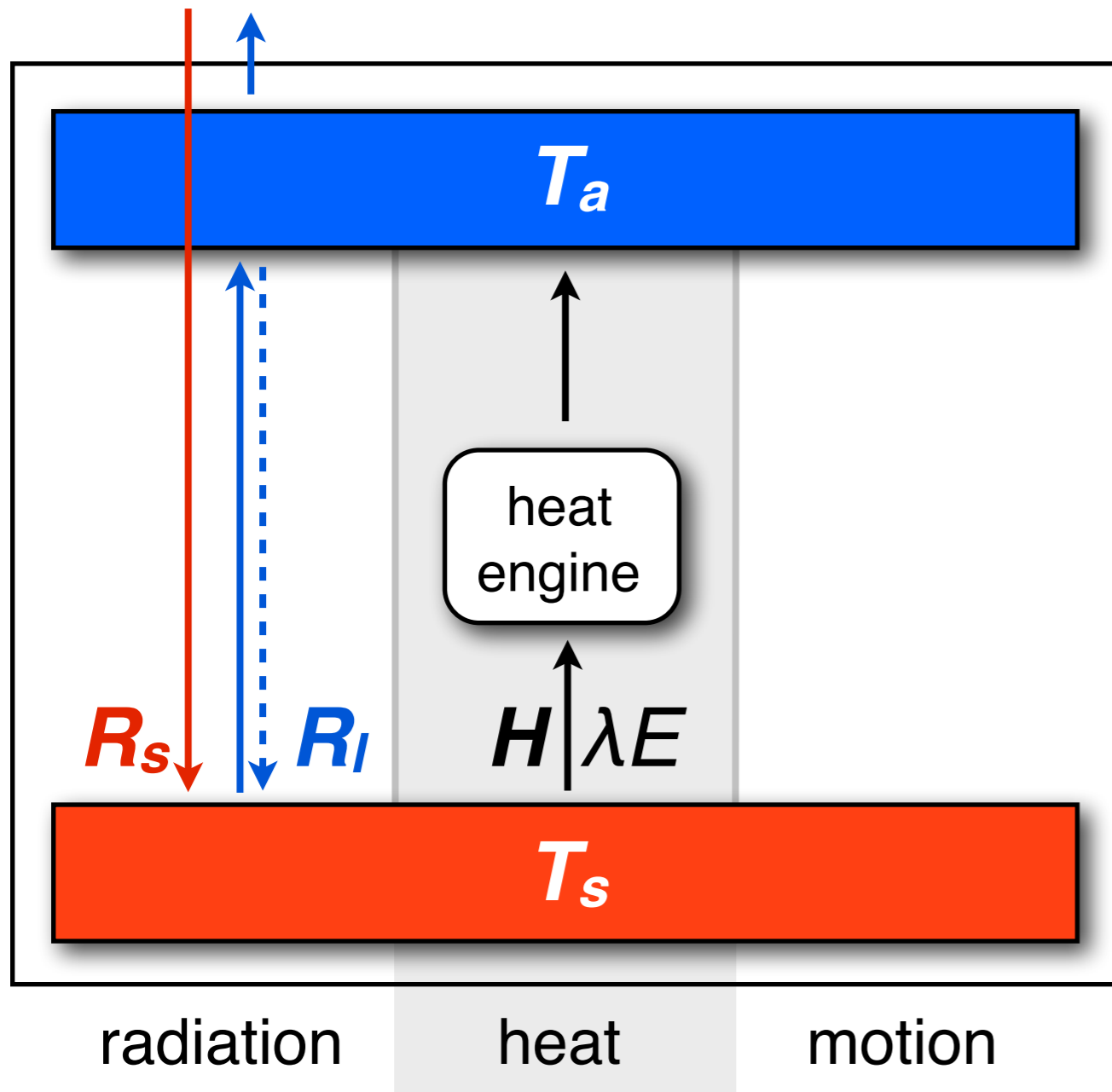
Perfection is achieved, not when there is nothing more to add, but when there is nothing left to take away.

Antoine de Saint-Exupery

Can we formulate a simple earth system model which captures the most important (thermo)dynamics to predict the response to radiative changes?

A simple climate model

energy balances as starting points



energy balances:

$$R_s - R_l - H - \lambda E = 0$$

$$R_s - \sigma T_a^4 = 0$$

R_s : absorbed solar radiation

R_l : net emission of terrestrial radiation

H : sensible heat flux

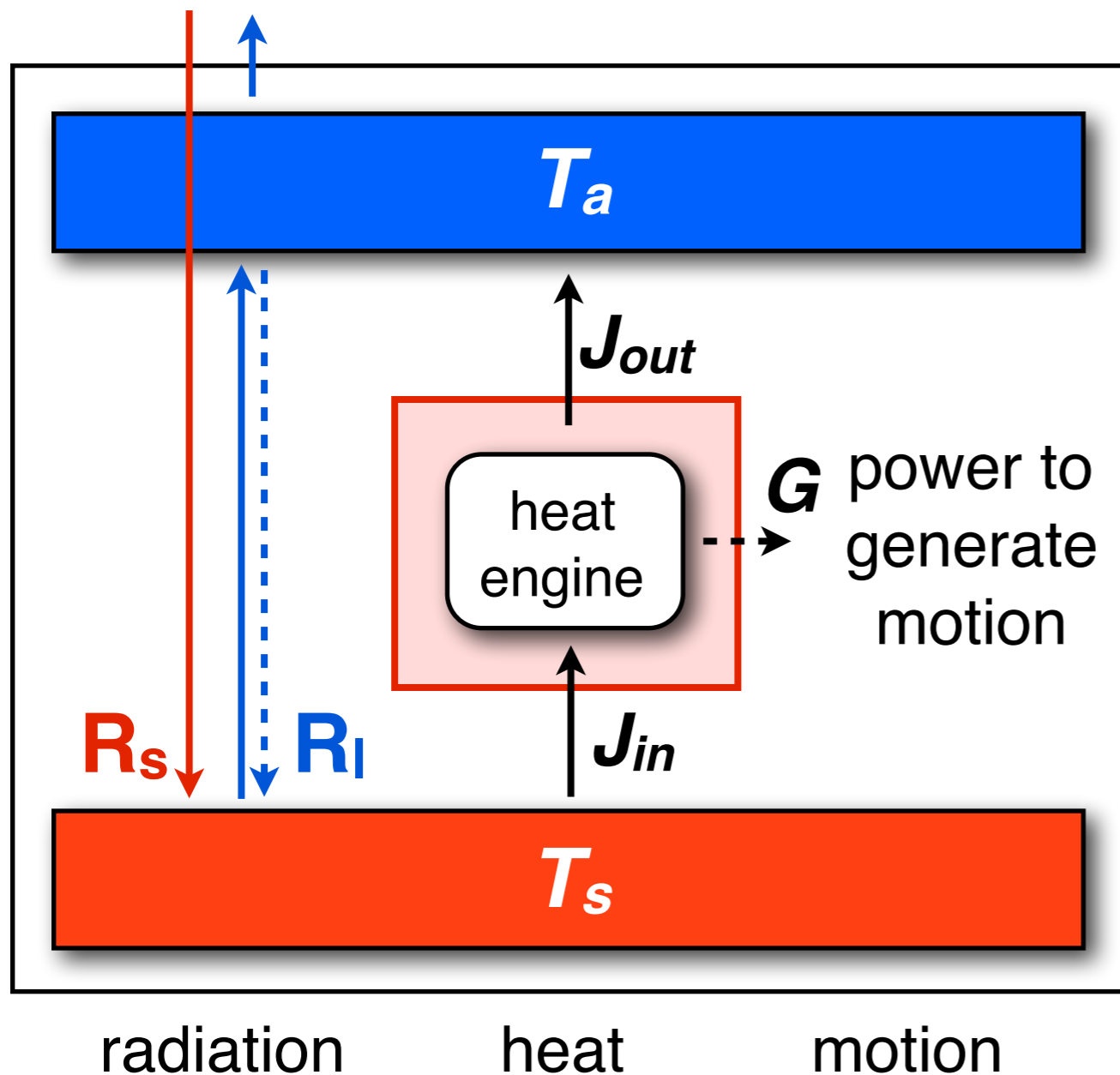
λE : latent heat flux

given: absorbed solar radiation R_s ($= 240 \text{ W m}^{-2}$) and surface temperature T_s ($= 288 \text{ K}$)

unknown: partitioning between R_l and $H + \lambda E$?

Atmospheric heat engine

thermodynamic limit on convective motion



first law: energy budget

$$0 = J_{in} - J_{out} - G$$

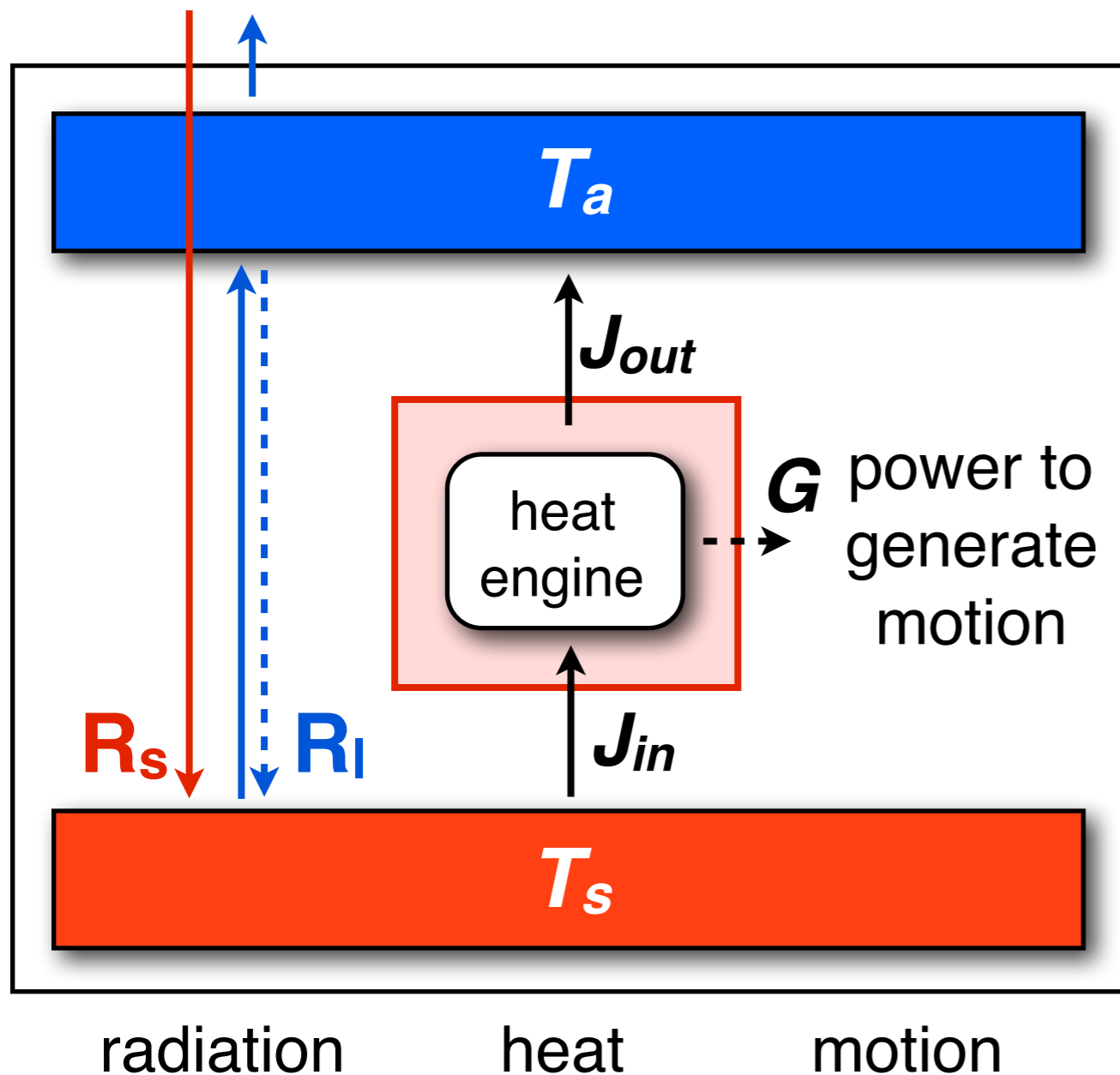
second law: entropy budget

$$\frac{J_{out}}{T_a} - \frac{J_{in}}{T_s} \geq 0$$

best case: $J_{out} = J_{in} \frac{T_a}{T_s}$

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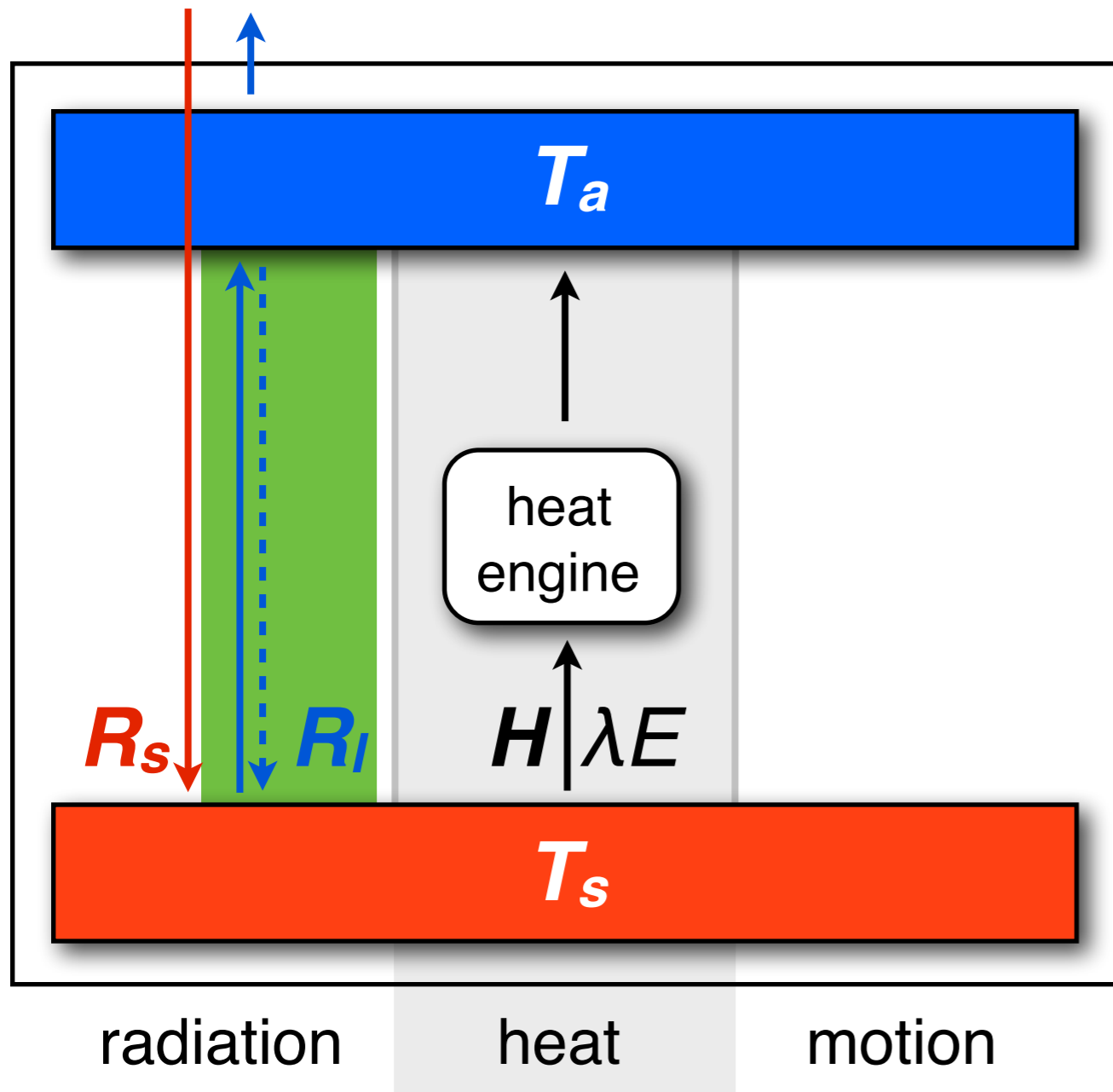
best case: $J_{out} = J_{in} \frac{T_a}{T_s}$

“Carnot” limit for G :

$$G = J_{in} \frac{T_s - T_a}{T_s}$$

A simple climate model

exchange of terrestrial radiation



assume **blackbody emission** for surface and atmosphere:

$$R_{l,s} = \sigma T_s^4$$

$$R_{l,a} = \sigma T_a^4$$

linearize emission:

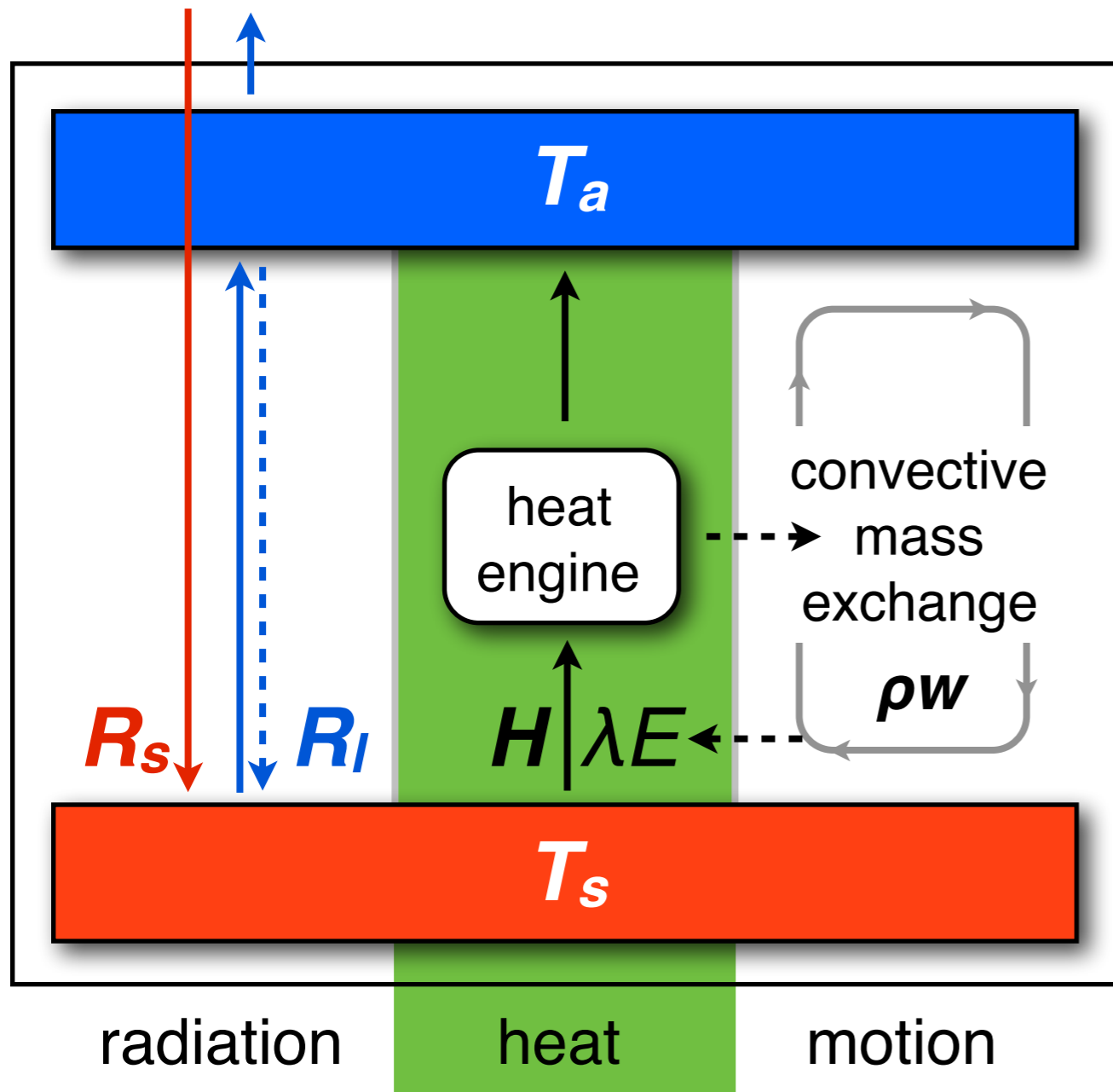
$$\sigma T^4 \approx R_0 + k_r (T - T_0)$$

results in simple expression for **net longwave radiative exchange**:

$$\begin{aligned} R_l &= R_{l,s} - R_{l,a} \\ &= k_r (T_s - T_a) \end{aligned}$$

A simple climate model

parameterization of heat fluxes



convective heat fluxes depend on a rate of **mass exchange**, ρw :

$$H = c_p \rho w (T_s - T_a)$$

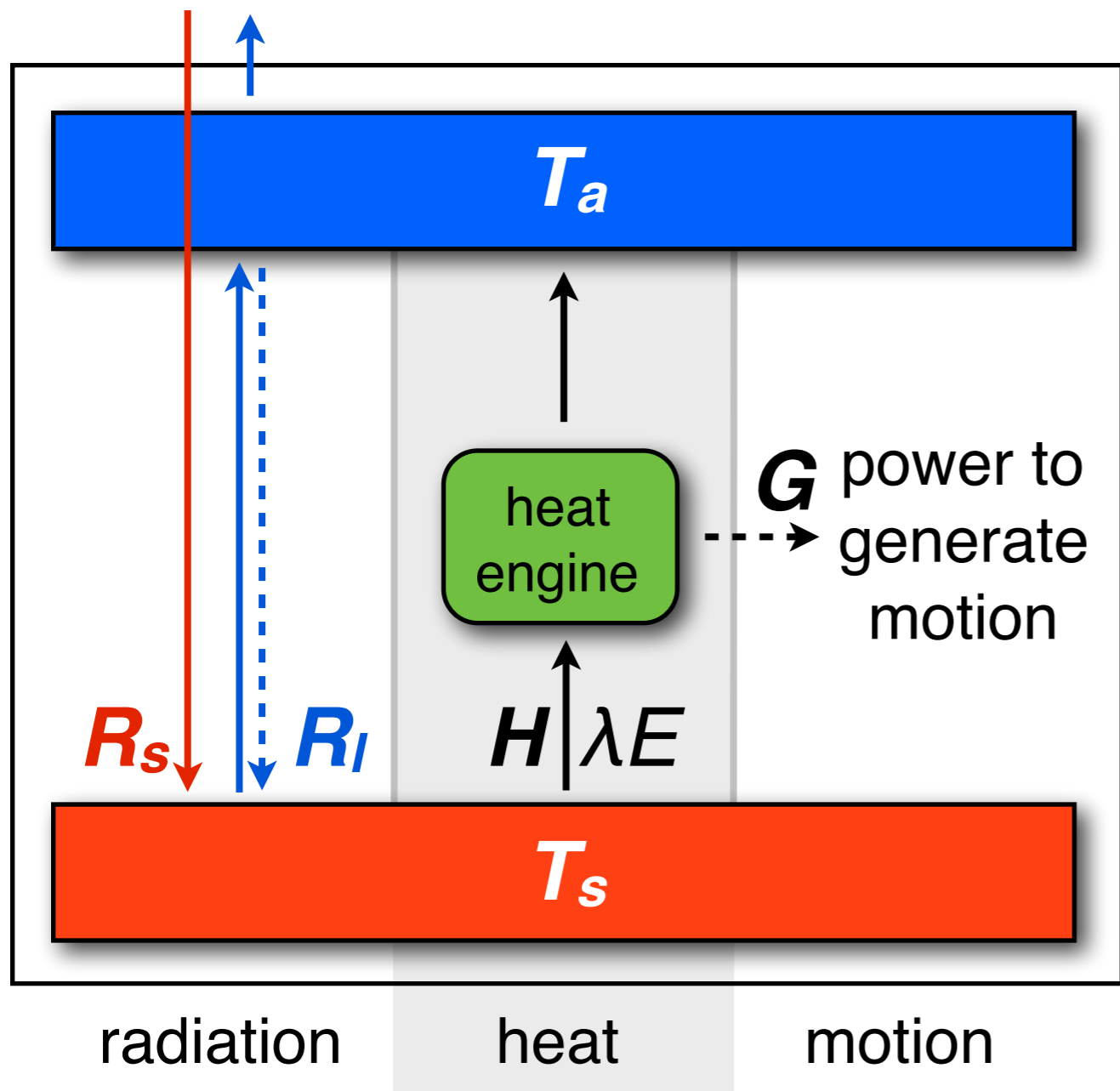
$$\lambda E = \lambda \rho w (q_s - q_a)$$

assume **saturation** for surface and atmosphere and **linearize** saturation vapor pressure curve with slope s

$$\lambda E = c_p \rho w \frac{s}{\gamma} (T_s - T_a)$$

$$\lambda E = \frac{s}{\gamma} H \quad \gamma: \text{ psychrometric constant}$$

Carnot limit for generating convection



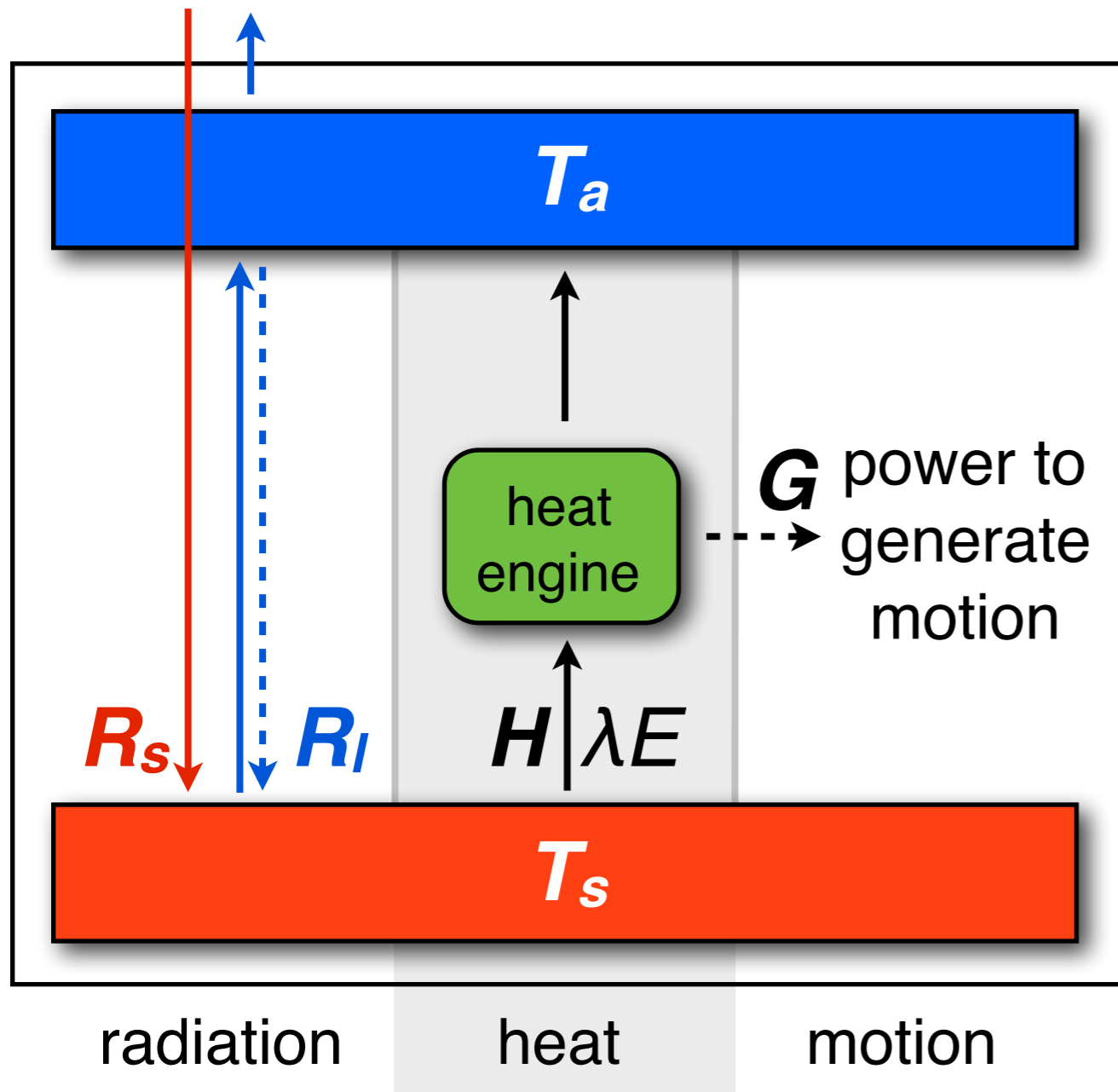
“Carnot” limit for G :

$$G = H \cdot \frac{T_s - T_a}{T_s}$$

use **surface energy balance** to express ΔT :

$$T_s - T_a = \frac{R_s - H - \lambda E}{k_r}$$

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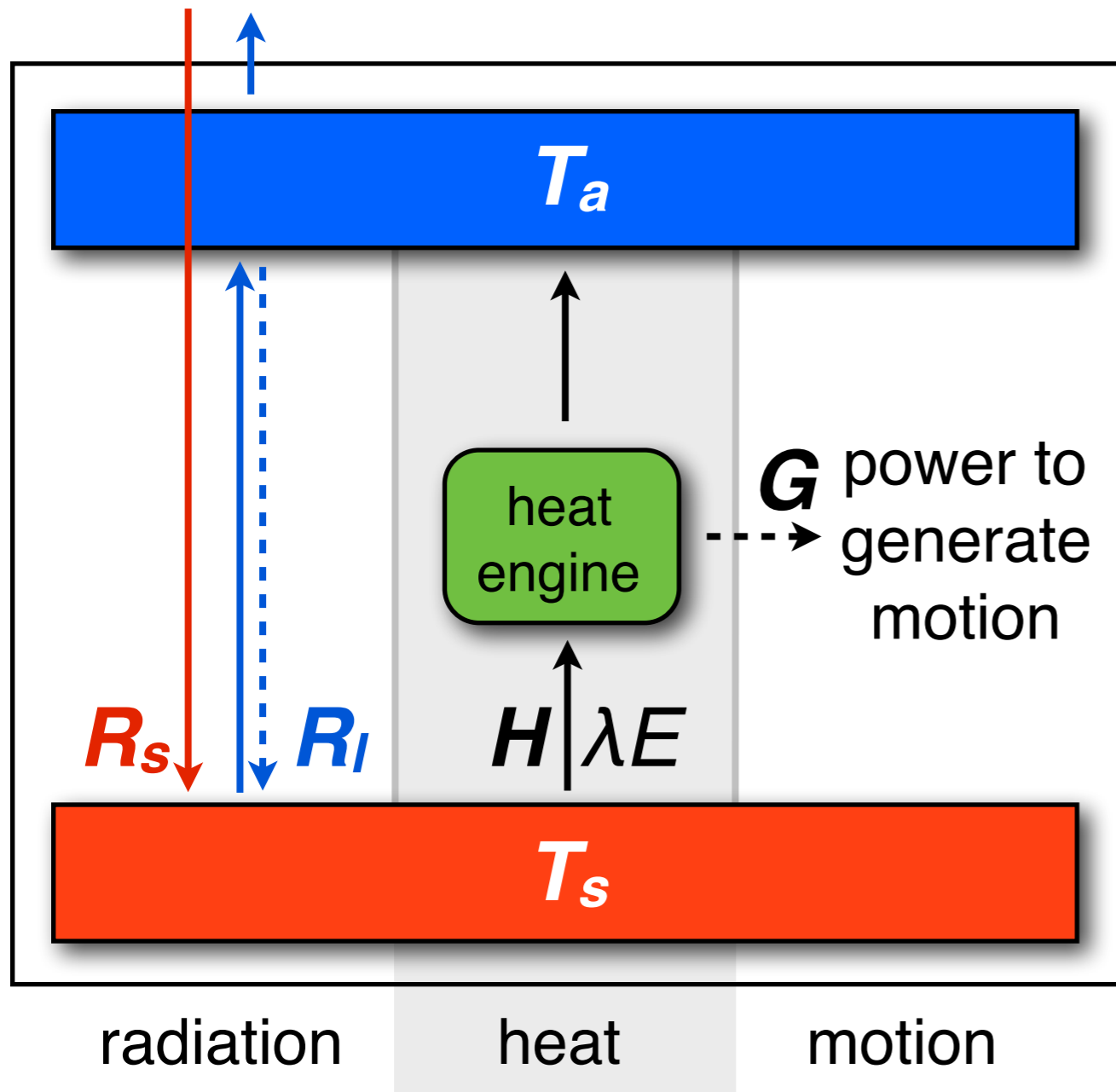
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maximize power G :

Carnot limit for generating convection



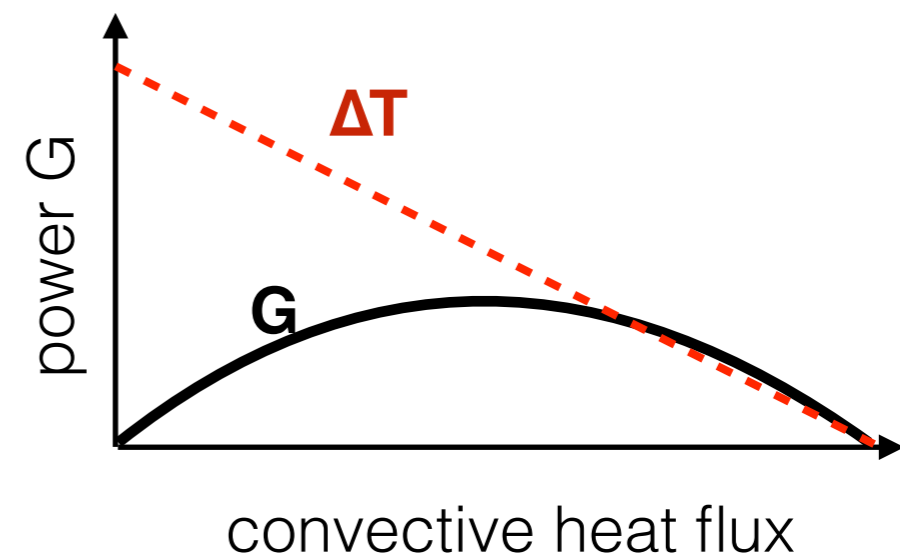
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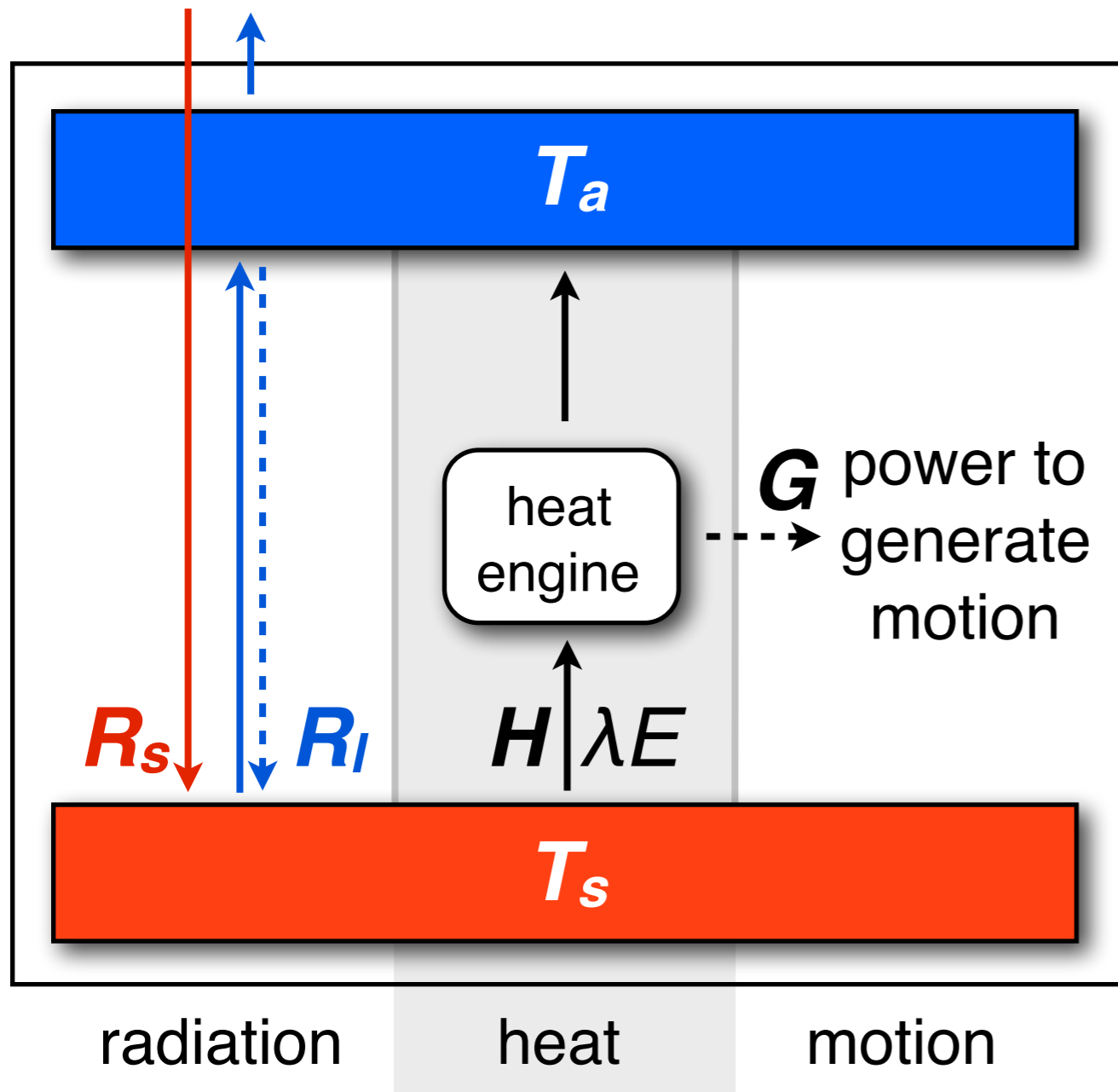
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maximize power G :



A simple climate model

flux partitioning at maximum convective power



max. power limit predicts **equal partitioning** among radiative and turbulent fluxes:

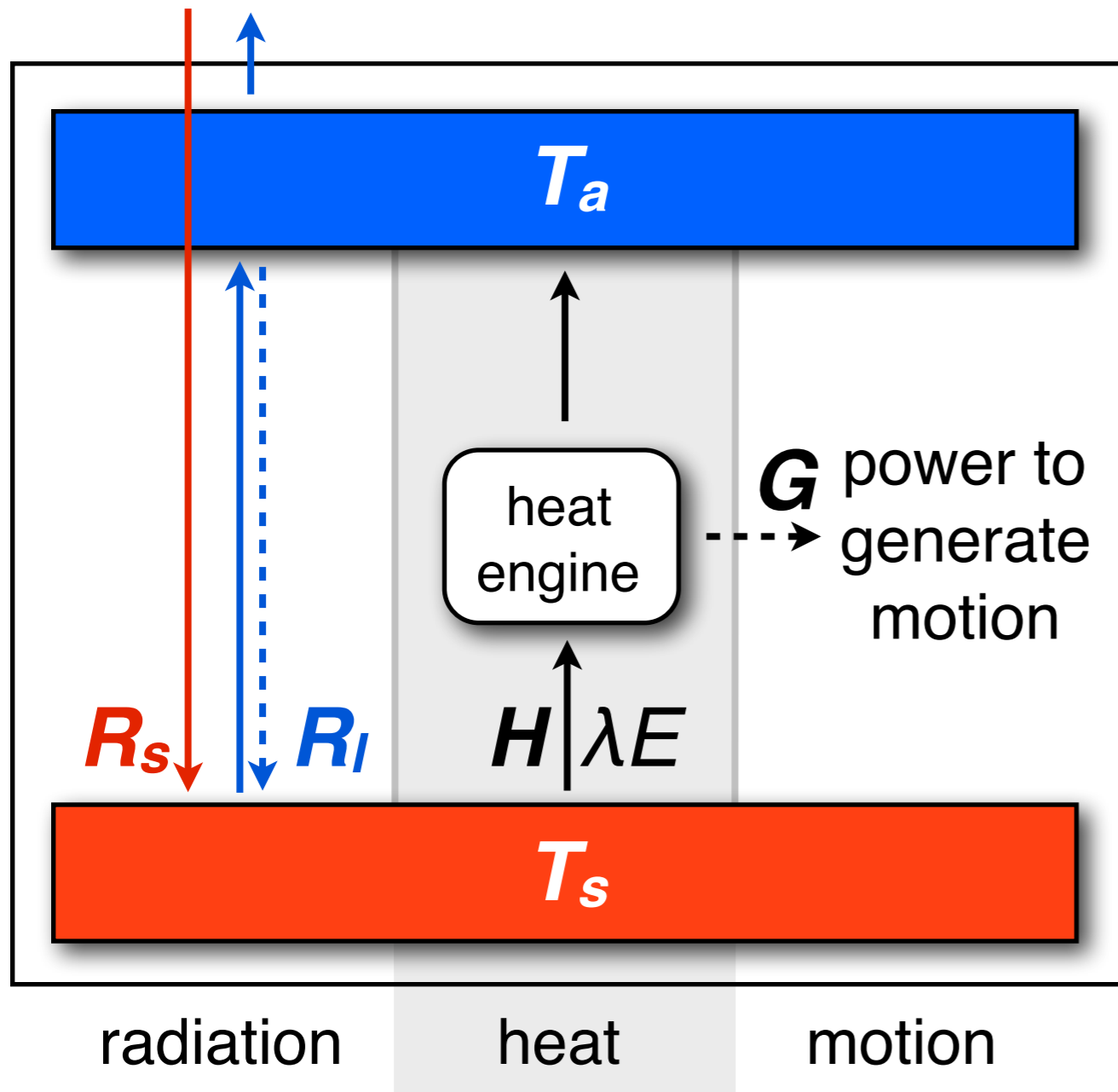
$$R_{l,opt} = \frac{R_s}{2}$$

$$H = \frac{\gamma}{s + \gamma} \frac{R_s}{2}$$

$$\lambda E = \frac{s}{s + \gamma} \frac{R_s}{2}$$

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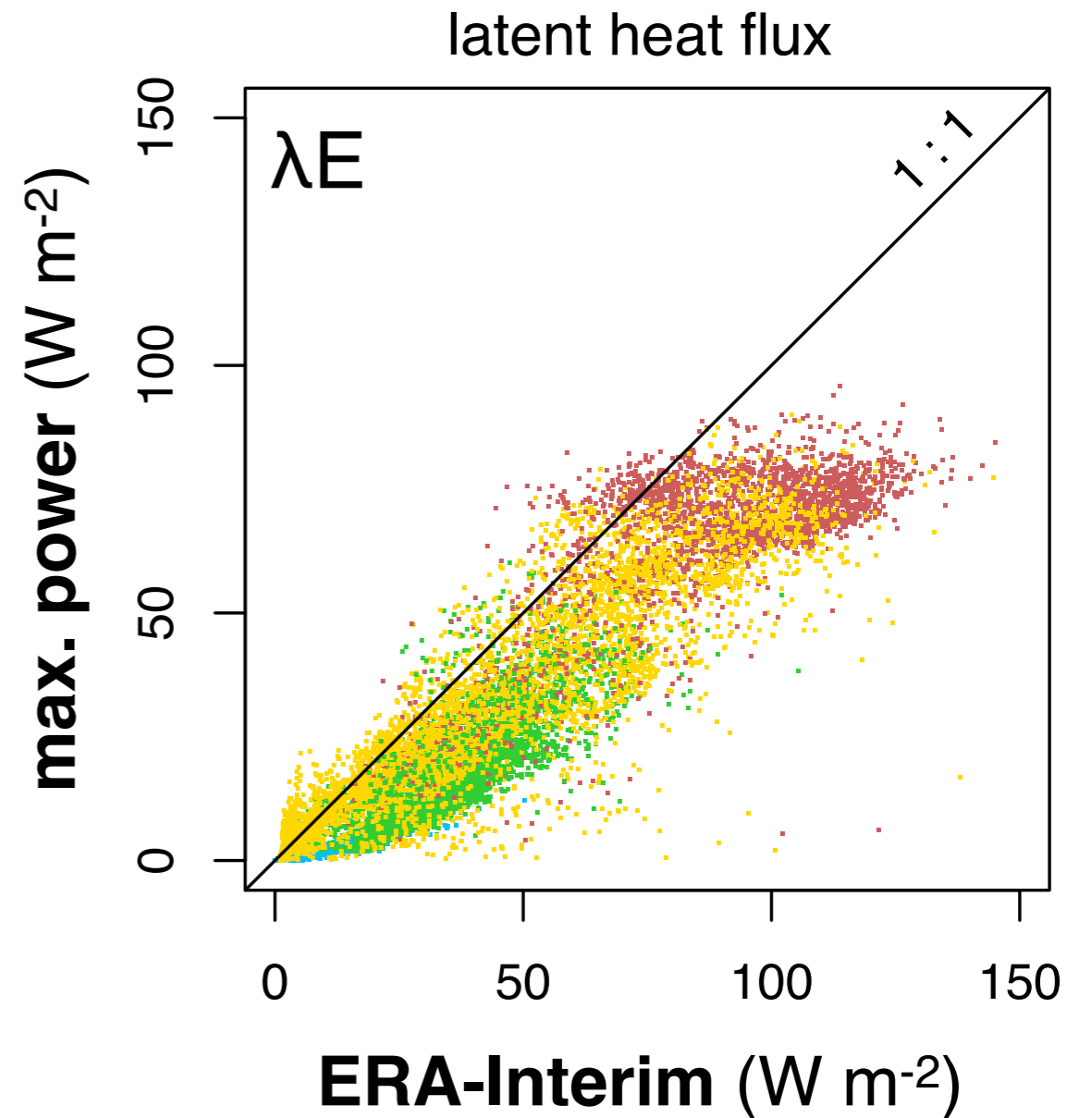
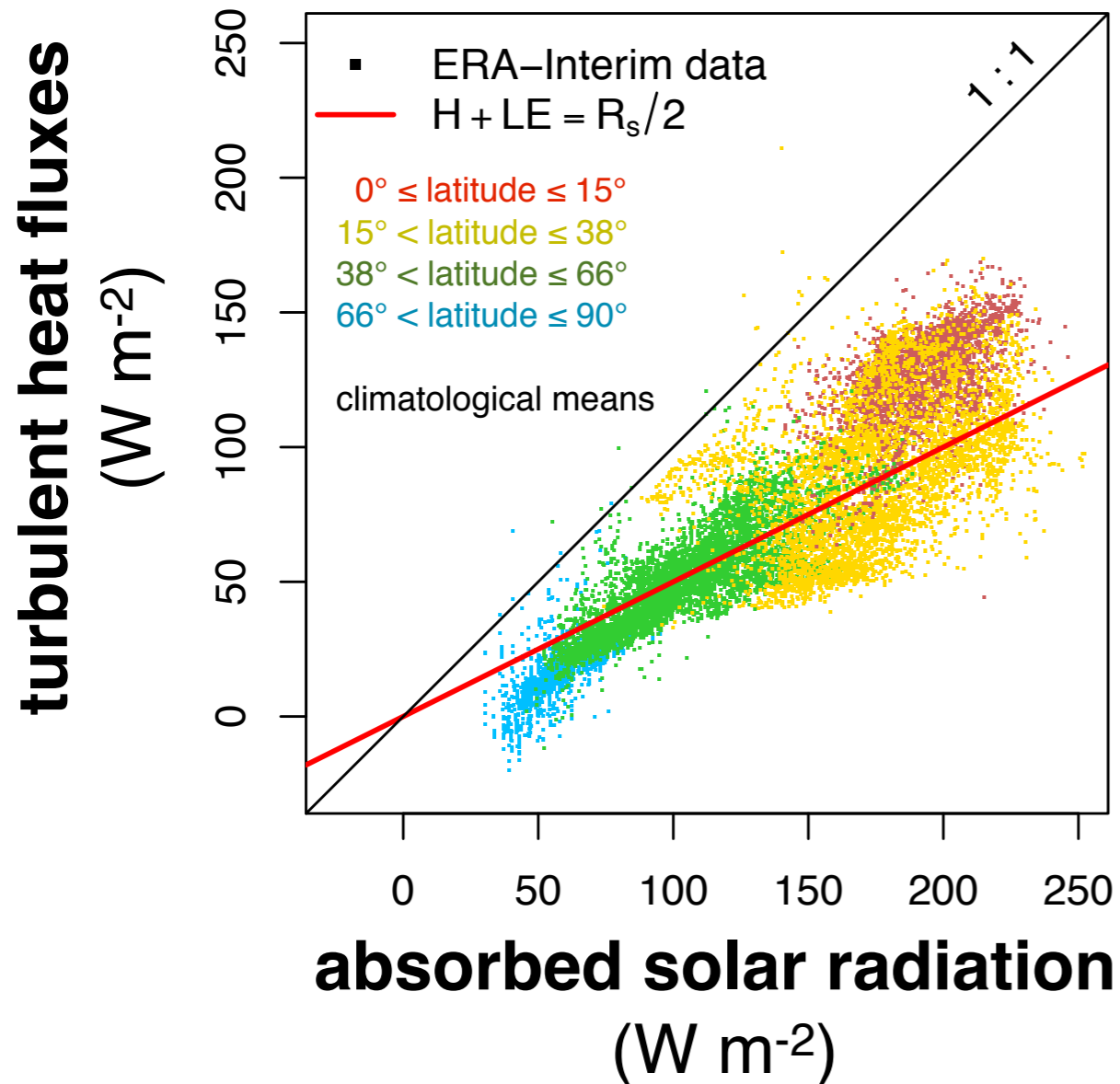
$$H = \frac{\gamma}{s + \gamma} \frac{R_s}{2}$$

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consistent with “equilibrium evaporation” rate of Schmidt (1909) and Slayter & McIlroy (1961), Priestley and Taylor (1971)

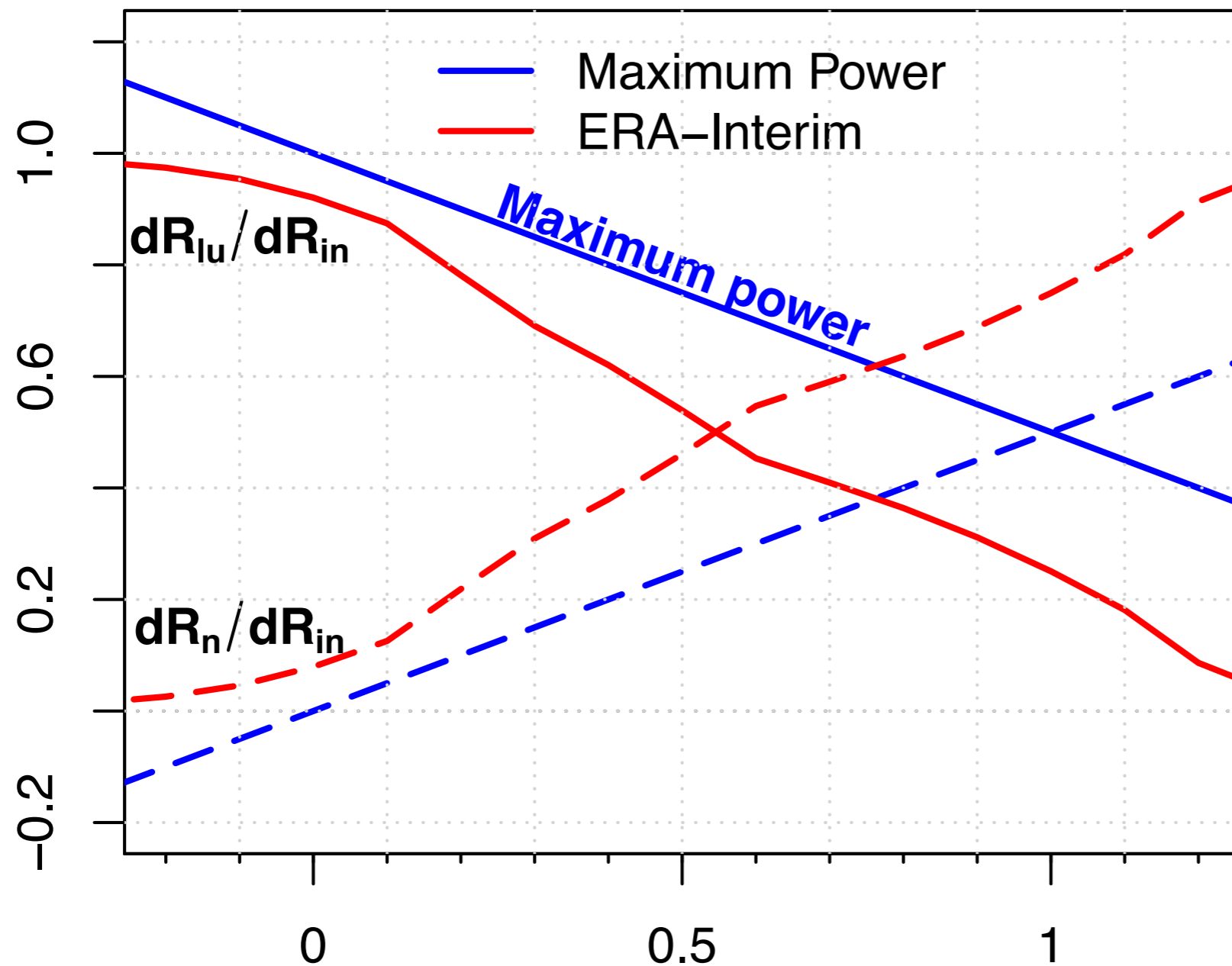
A simple climate model

surface energy partitioning on land (with added water balance constraint)



Sensitivity to type of radiative forcing

Sensitivity to total incoming radiation R_{in}



$$\begin{aligned}
 R_{ln} &= R_{sn}/2 \\
 &= R_{lu}(T_s) - R_{ld} \\
 \partial R_{lu}/\partial R_{ld} &= 1 \\
 \partial R_{lu}/\partial R_{sn} &= 1/2
 \end{aligned}$$

longwave change dominates

$\Delta R_{sn}/\Delta R_{in}$

shortwave change dominates

Hydrologic Cycling and Surface Warming

Evaporation rate:

$$\lambda E_{opt} = \frac{s}{\gamma + s} \frac{R_s}{2}$$

Kleidon and Renner (2013) *ESD*
Kleidon, Kravitz, Renner (2015) *GRL*

Hydrologic Cycling and Surface Warming

Evaporation rate:

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Relative sensitivity:

$$\frac{1}{E} \Delta E = \frac{1}{E} \frac{\partial E}{\partial s} \frac{ds}{dT_s} \Delta T_s + \frac{1}{E} \frac{\partial E}{\partial R_s} \Delta R_s$$

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$\approx 2.2 \% \text{ K}^{-1}$ $\approx 1 \% \text{ K}^{-1}$

**greenhouse-
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warming:
2.2 % K⁻¹**

**solar-induced
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Hydrologic Cycling and Surface Warming

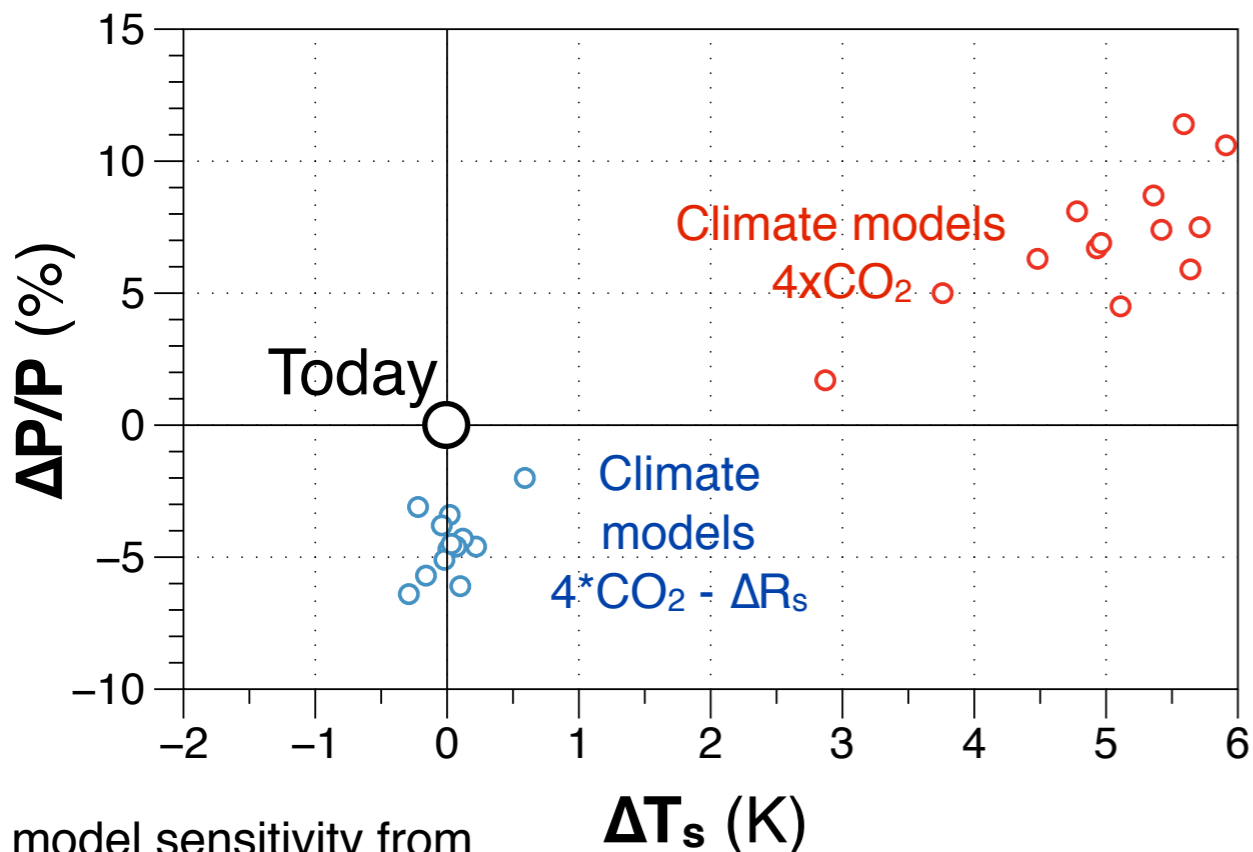
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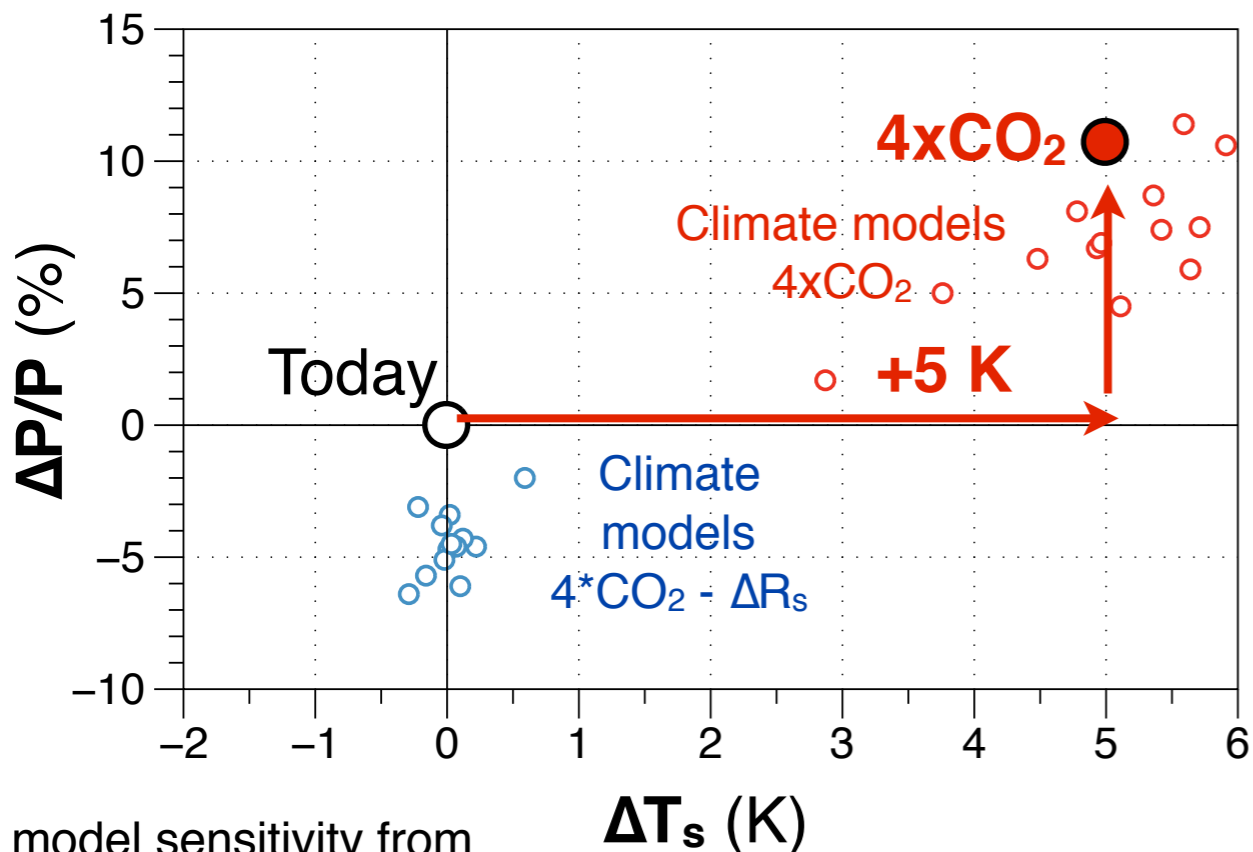
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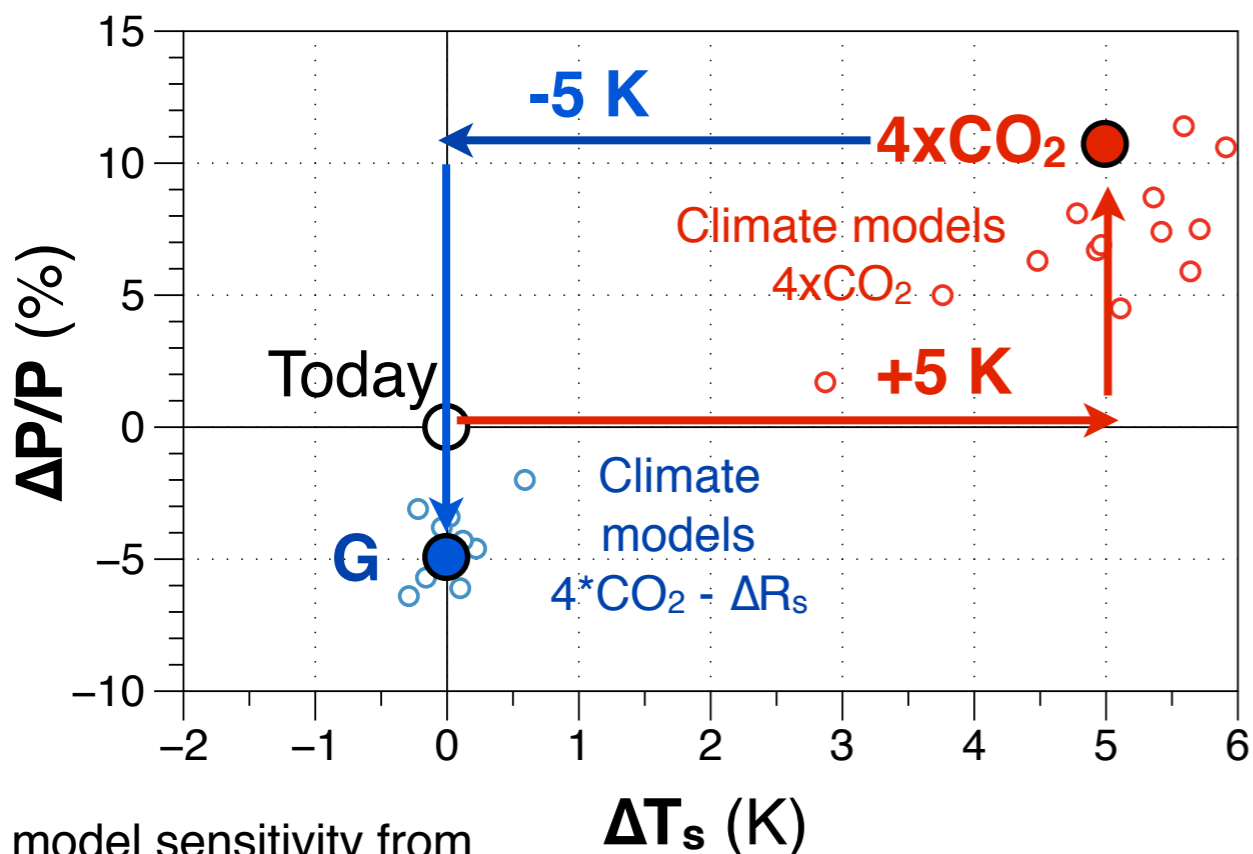
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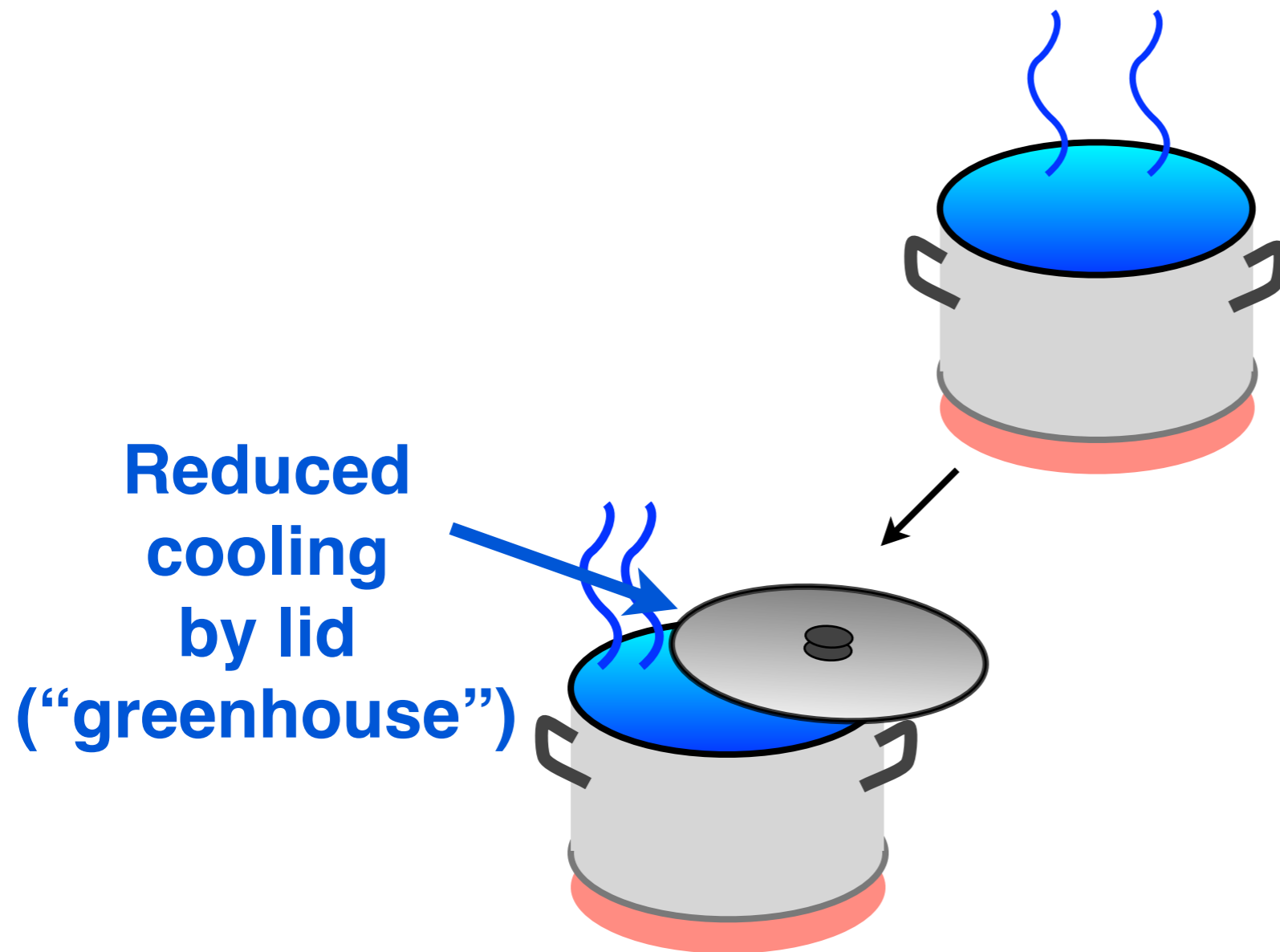
Hydrologic Cycling and Surface Warming

Analogy: Increasing the temperature of a pot on a stove



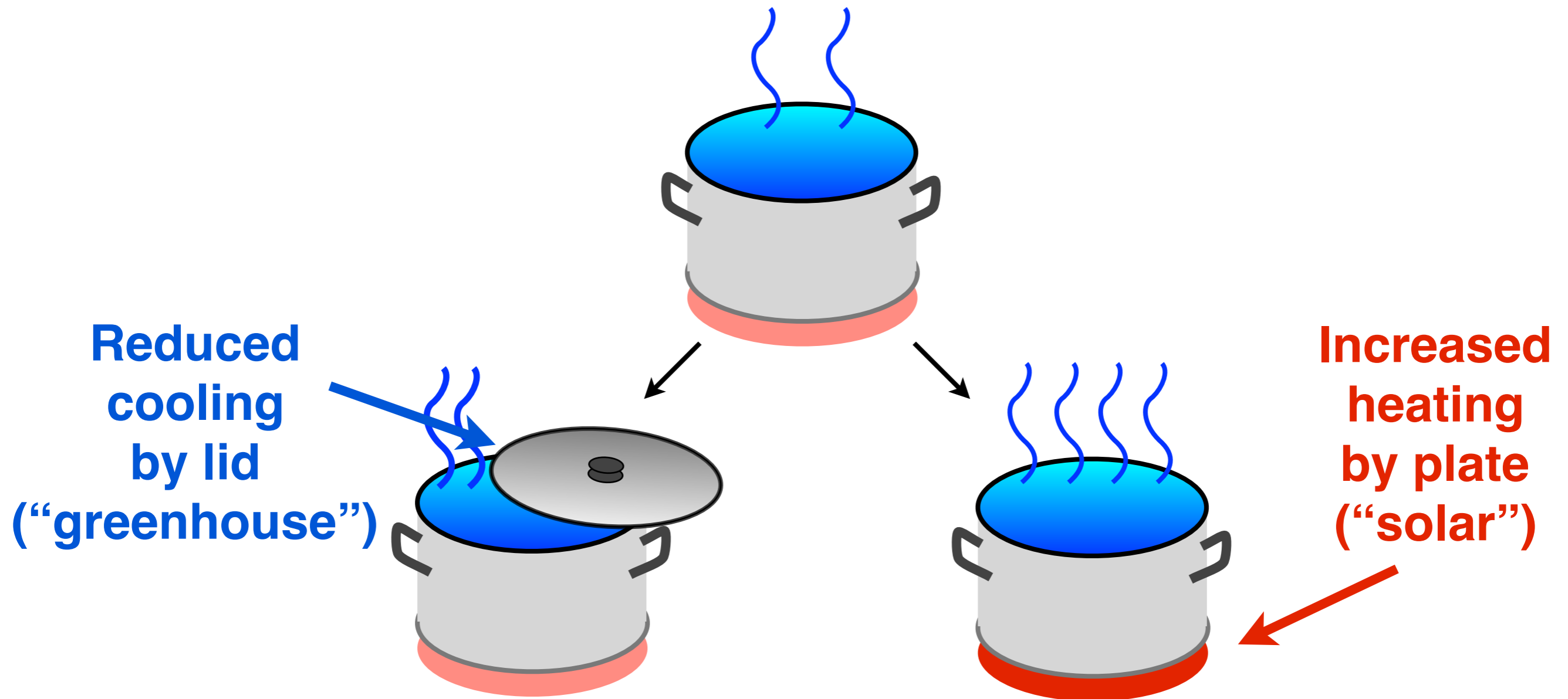
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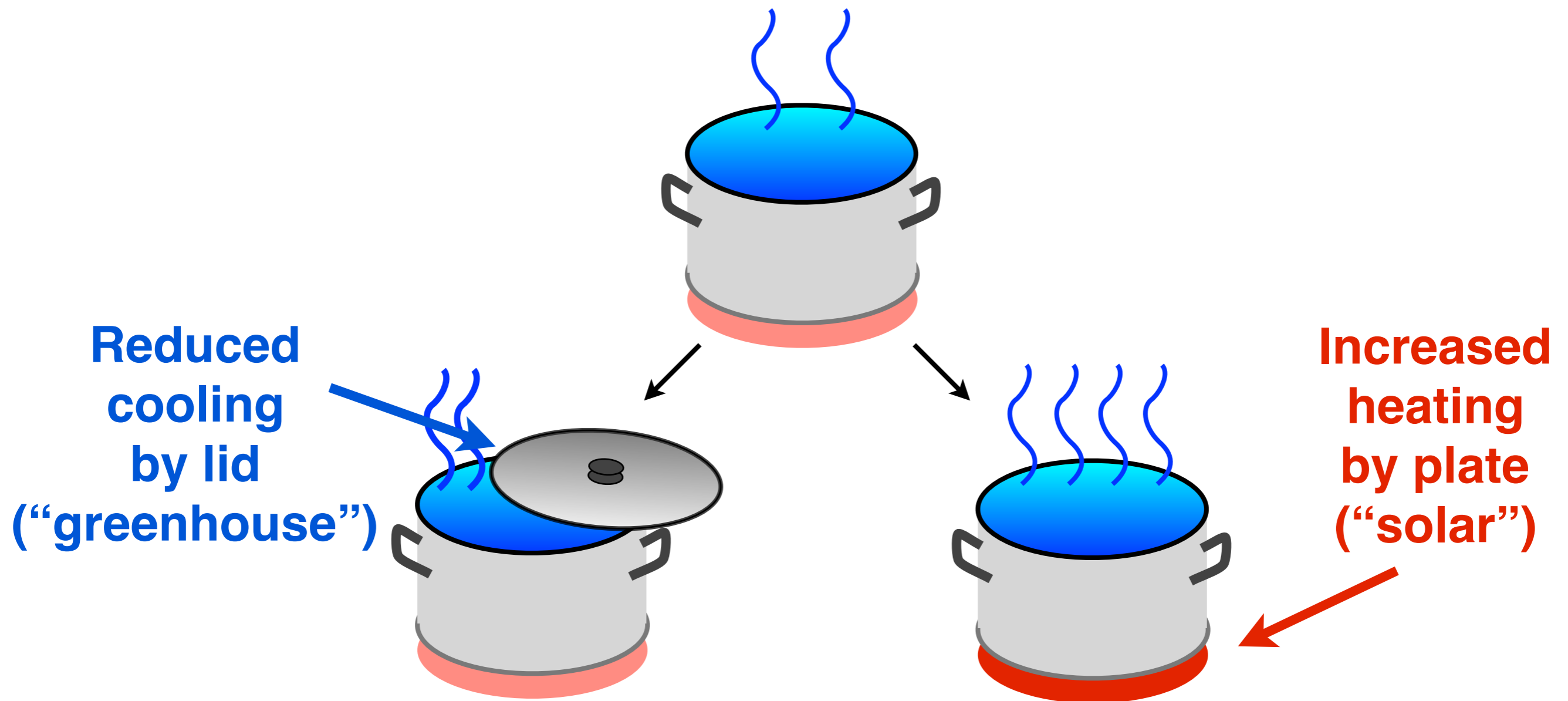
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Hydrologic Cycling and Surface Warming

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Solar geoengineering:

Compensate temperature increase by lid by reducing the heating

Summary and Conclusions

Earth systems' approach

- atmosphere as a heat engine
- trade-off between temperature gradient and the turbulent heat flux
- thermodynamic optimality - state of maximum power
- allows first order predictions on earth system

Conclusion:

- type of radiative change (SW \leftrightarrow LW) is key to predict response of temperature and water cycle
- 2.2% / K increase of water cycle by greenhouse warming understood by saturation vapour pressure constrained by surface energy balance

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Thank you!